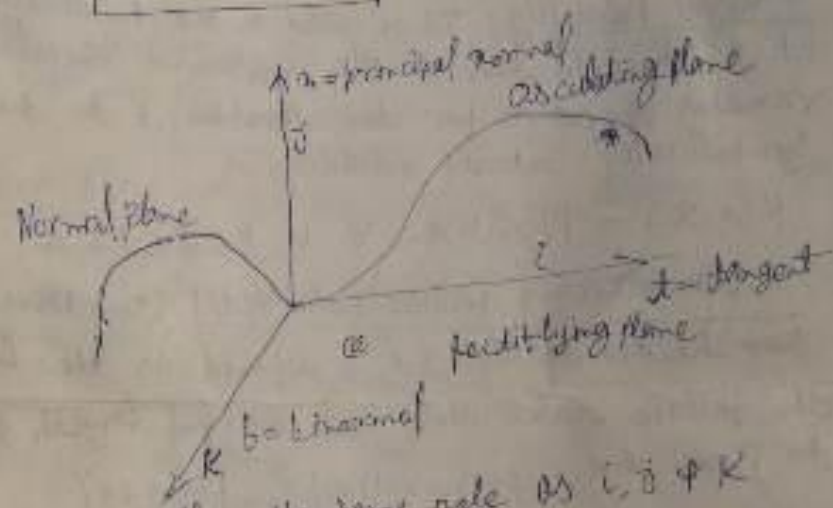


Equation of normal plane - "osculating plane"

where r = position vector of current point
 r_1 = position vector of any point
 and t = tangent vector of any point

$$t = \frac{dr}{dt} = \frac{dr_1}{dt} \text{ or } \dot{r} = \dot{r}_1$$

$$\Rightarrow (r - r_1) \cdot \dot{r} = 0$$



t, n, b obey the same rule as i, j, k

$$t \times t = n \cdot n = b \cdot b = 1$$

$$t \cdot n = n \cdot b = b \cdot t = 0$$

and $t \times n = b, n \times b = t, b \times t = n$

$$t \times t = t \times b = n \times n = 0$$

Principal Normal: - The plane which is \perp to tangent is called principal normal

or, The plane which is lying in osculating plane is called principal normal.

Binormal: - The normal which is perpendicular to principal normal is called binormal, it is denoted by b

or, The normal which lying in normal plane is called binormal

or, The normal which is perpendicular to osculating plane is called binormal.

Osculating plane:- The plane which contains r & t is called ⁽²⁾ osculating plane.
 or, The plane which is \perp to binormal is called osculating plane whose eqⁿ is

$$(r-r) \cdot b = 0$$

Normal plane:- The plane which contains r & b is called normal plane.
 or, The plane which is \perp to tangent is called normal plane. whose eqⁿ is

$$(r-r) \cdot t = 0$$

Rectifying plane:- The plane which contains b & t is called rectifying plane.
 or, The plane which is \perp to principal normal is called rectifying plane. whose eqⁿ is

$$(r-r) \cdot n = 0$$

- Notes:-
- (i) Eqⁿ of tangent plane is $r = r + t \cdot dt$
 - (ii) Eqⁿ of normal plane is $r = r + t \cdot dt$
 - (iii) Eqⁿ of binormal plane is $r = r + t \cdot dt$

Curvature and Torsion:-
 Curvature: Differentiation of 'w.r.t. 's' is called curvature vector whose magnitude is denoted by

$$K \quad \text{i.e.} \quad K = \left| \frac{dt}{ds} \right|$$

The reciprocal of curvature is called radius of curvature which is denoted by ρ

$$\text{i.e.} \quad \rho = \frac{1}{K}$$

$$\Rightarrow \rho K = 1$$